

# **MATHEMATICS 31**

**Mr. M Cherney**



# **COURSE OUTLINE 2025-2026**

Ch 1 Algebra	9(11 1 <sup>st</sup> FR)-8 Classes	9(11) School Days	Sept 2 – Sept 24
Ch 2 Limits	7-5 Classes	7 School Days	Oct 1 – Oct 20
Ch 3 Derivatives	9-7 Classes	9 School Days	Oct 26 – Nov 12
Ch 4 Advanced Derivatives	9-5 Classes	9 School Days	Nov 17 – Dec 3
Ch 5 Curve Sketching	14-7 Classes	14 School Days	Dec 8 – Feb 4
Ch 6 Derivative Applications	9-6 Classes	9 School Days	Feb 9 – Mar 4
Ch 7 Antiderivatives	11-8 Classes	11 School Days	Mar 9 – Apr 15
Ch 8 Integration Applications	6-5 Classes	6 School Days	Apr 20 – Apr 29
Course Review/Final	14(16 OE)-12 Classes	14(16) School Days	May 4 – June 12
	88(63) Classes	88(92) School Days	

Final

## Final Exam

May 4 – June 12

## COURSE MARKING    2025-2026

Heading	Date	Weight	Points Earned (%)	Percent (%)
<b>Course Work</b>		70		
<b>Tests</b>		95		
Chapter 1 Algebra		10		
Chapter 2 Limits		10		
Chapter 3 Derivatives		15		
Chapter 4 Advanced Derivatives		10		
Chapter 5 Curve Sketching		15		
Chapter 6 Derivative Applications		15		
Chapter 7 Antiderivatives		15		
Chapter 8 Integration Applications		10		
<b>Homework</b>		5		
<b>Final Exam</b>		30		
<b>Final Grade</b>				

**Daily Homework** for each assignment is due the day after it is assigned and at the latest the day of the test for that chapter. It will be marked for completeness, 1 mark for each completed question out of the total assigned questions. Incorrect questions should be corrected.

**Review Summary Sheets** are given for each chapter and can be used as 'I Can' statements to self assess learning or as review sheets for content covered in the chapter.

**Tests** may be rewritten on a chapter which will be scheduled on the day before the next chapter test. Your best score up to 79% will be taken on rewrites.

**Extra Help** or a quiet place to work is available during any lunch hour in my room through out the year on a come and go as you need help basis.

## Extra Practice

From Text Book

Chapter 1	Lesson 2	Pg 66 Question 1
	Lesson 3	Pg 67 Questions 1 – 2
	Lesson 4	Pg 206 Questions 1 – 2
	Lesson 5	Pg 163 Questions 1 – 2
	Lesson 8	Pg 166 Questions 1 – 2
		Pg 116 Questions 1 – 2
		Pg 267 – 269 Questions 1 – 3, 5
		Pg 273 – 275 Questions 2, 3, 5, 6, 7, 8, 10, 11
		Pg 279 – 280 Questions 5, 7, 8, 10, 11
		Pg 284 – 287 Questions 1, 3, 7, 11, 13, 15, 19, 20, 23, 27, 29, 35, 40, 45, 56
		Pg 291 – 292 Questions 1 – 4
Chapter 2	Lesson 1	Pg 56 – 57 Questions 1 – 5
	Lesson 2	Pg 50 – 51 Questions 1 – 6, 8
	Lesson 4	Pg 18 – 20 Questions 1 – 6
		Pg 27 – 29 Questions 1 – 4, 6, 8, 12
		Pg 9 – 10 Questions 7 – 11
		Pg 35 Question 7
		Pg 43 – 44 Questions 1, 3, 8
Chapter 3	Lesson 1	Pg 75 – 77 Questions 1 – 7, 9, 11
	Lesson 2	Pg 83 – 84 Questions 1 – 4, 7 – 9
	Lesson 3	Pg 88 – 89 Questions 1, 4, 6 – 9
	Lesson 4	Pg 92 – 93 Questions 2, 6 – 8
	Lesson 5	Pg 95 – 96 Questions 2, 4, 7, 8
	Lesson 6	Pg 102 – 103 Questions 1, 3 – 5, 7, 9, 10
	Lesson 7	Pg 107 – 108 Questions 1 – 3
		Pg 111 Questions 1 – 7
Chapter 4	Lesson 1	Pg 306 – 307 Questions 1 – 38 even
	Lesson 2	Pg 313 – 315 Questions 1 – 5, 7, 8
	Lesson 3	Pg 319 – 320 Questions 1 – 3, 9
	Lesson 5	Pg 361 – 362 Questions 4, 5, 7
		Pg 366 – 368 Questions 1, 3 – 11
		Pg 375 – 376 Questions 3 – 10, 17, 18
		Pg 383 – 384 Questions 1 – 8

Chapter 5	Lesson 2	Pg 170 – 171 Questions 1 – 5 Pg 176 – 177 Questions 1, 2, 4 – 8 Pg 182 Questions 1, 3, 4, 6 Pg 229 – 230 Questions 1 – 3, 6 – 8 Pg 240 Questions 1 – 3, 7, 9, 12 Pg 232 Questions 1 – 3
	Lesson 3	Pg 229 – 230 Questions 1 – 3, 6 – 8 Pg 240 Questions 1 – 3, 7, 9, 12
	Lesson 4	Pg 232 Questions 1 – 3 Pg 188 – 191 Questions 1 – 20 odd Pg 212 – 213 Questions 1 – 5
	Lesson 5	Pg 222 – 223 Questions 1, 2, 4 – 6, 8 – 11
	Lesson 6	Pg 244 Questions 1 – 3
Chapter 6	Lesson 1	Pg 188 – 191 Questions 1 – 20 odd
	Lesson 2	Pg 124 – 126 Questions 1 – 9
	Lesson 3	Pg 128 – 129 Questions 1 – 9 Pg 134 – 135 Questions 1 – 9
	Lesson 4	Pg 145 – 146 Questions 1 – 17 Pg 139 – 140 Questions 1 – 6 Pg 195 – 196 Questions 1 – 8
	Lesson 5	Pg 390 – 392 Questions 1 – 14 even
	Lesson 6	Pg 152 Questions 1 – 8
Chapter 7	Lesson 1	Pg 408 – 409 Questions 1 – 5
	Lesson 3	Pg 411 – 412 Questions 1, 2, 3, 5, 6 Pg 415 Questions 1 – 5 Pg 420 – 421 Questions 1 – 7
	Lesson 4	Pg 437 – 438 Questions 1, 2, 3, 7 Pg 454 – 455 Questions 1 – 3 Pg 465 – 466 Questions 1 – 4
	Lesson 5	Pg 500 Questions 2 – 5 Pg 505 – 506 Questions 1 – 4
	Lesson 7	Pg 461 Question 1
Chapter 8	Lesson 1	Pg 474 – 475 Questions 1 – 3
	Lesson 2	Pg 500 Questions 2 – 5 Pg 511 – 512 Questions 3, 4

# CALCULUS FORMULA SHEET

Graphing Calculator Window Format

$$x[x_{\min}, x_{\max}, x_{\text{scl}}] \quad y[y_{\min}, y_{\max}, y_{\text{scl}}]$$

## Properties of Limits

$$\lim_{x \rightarrow a} [f(x) + g(x)] = \lim_{x \rightarrow a} f(x) + \lim_{x \rightarrow a} g(x)$$

$$\lim_{x \rightarrow a} [f(x) - g(x)] = \lim_{x \rightarrow a} f(x) - \lim_{x \rightarrow a} g(x)$$

$$\lim_{x \rightarrow a} [cf(x)] = c \lim_{x \rightarrow a} f(x)$$

$$\lim_{x \rightarrow a} [f(x)g(x)] = \lim_{x \rightarrow a} f(x) \lim_{x \rightarrow a} g(x)$$

$$\lim_{x \rightarrow a} \left[ \frac{f(x)}{g(x)} \right] = \frac{\lim_{x \rightarrow a} f(x)}{\lim_{x \rightarrow a} g(x)}$$

$$\lim_{x \rightarrow a} [f(x)]^n = \left[ \lim_{x \rightarrow a} f(x) \right]^n, n > 0$$

$$\lim_{x \rightarrow a} \sqrt[n]{f(x)} = \sqrt[n]{\lim_{x \rightarrow a} f(x)}$$

$$\lim_{x \rightarrow a} c = c \quad \lim_{x \rightarrow a} x = a$$

$$\lim_{x \rightarrow a} x^n = a^n \quad \lim_{x \rightarrow a} \sqrt[n]{x} = \sqrt[n]{a}$$

$$\lim_{x \rightarrow a} P(x) = P(a)$$

$$\lim_{x \rightarrow a} \frac{P(x)}{Q(x)} = \frac{P(a)}{Q(a)}$$

if  $\lim_{x \rightarrow a^-} f(x) \neq \lim_{x \rightarrow a^+} f(x)$ ,

then  $\lim_{x \rightarrow a} f(x)$  does not exist

if  $\lim_{x \rightarrow a^-} f(x) = L = \lim_{x \rightarrow a^+} f(x)$ ,

then  $\lim_{x \rightarrow a} f(x) = L$

$$\lim_{n \rightarrow \infty} \left( \frac{1}{n} \right)^r = 0, \quad r > 0$$

$$\lim_{n \rightarrow \infty} r^n = 0, \quad |r| < 1$$

$$\lim_{n \rightarrow \infty} S_n = \frac{a}{1-r}, \quad |r| < 1$$

## Properties and Rules of Derivatives

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$\frac{d}{dx}(c) = 0$$

$$\frac{d}{dx}[cf(x)] = c \frac{d}{dx} f(x)$$

$$\frac{d}{dx}[f(x) + g(x)] = \frac{d}{dx} f(x) + \frac{d}{dx} g(x)$$

$$\frac{d}{dx}[f(x) - g(x)] = \frac{d}{dx} f(x) - \frac{d}{dx} g(x)$$

$$\frac{d}{dx}[f(x)g(x)] = f(x) \frac{d}{dx} g(x) + g(x) \frac{d}{dx} f(x)$$

$$\frac{d}{dx} \left[ \frac{f(x)}{g(x)} \right] = \frac{g(x) \frac{d}{dx} f(x) - f(x) \frac{d}{dx} g(x)}{[g(x)]^2}$$

$$\frac{d}{dx}[f(g(x))] = f'(g(x)) \frac{d}{dx} g(x)$$

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}[g(x)]^n = n[g(x)]^{n-1} g'(x)$$

$$s = f(t)$$

$$v = \frac{ds}{dt} = f'(t)$$

$$a = \frac{dv}{dt} = \frac{d^2 s}{dt^2} = f''(t)$$

## Newton's Method

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$

## Curve Sketching

if  $f'(x) > 0$  on  $I$ , then  $f$  is increasing on  $I$   
 if  $f'(x) < 0$  on  $I$ , then  $f$  is decreasing on  $I$

$f'(x) = 0$  is a local max or min  
 or critical number

$\lim_{x \rightarrow a} f(x) = \pm\infty$  is a vertical asymptote

$\lim_{x \rightarrow \pm\infty} f(x) = L$  is a horizontal asymptote

if  $f''(x) > 0$  on  $I$ ,  
 then  $f$  is concave up on  $I$

if  $f''(x) < 0$  on  $I$ ,  
 then  $f$  is concave down on  $I$

if  $f''(x) = 0$  on  $I$ ,  
 then  $x$  is a possible inflection point

if  $f'(c) = 0$  and  $f''(c) > 0$ ,  
 then  $c$  is a local minimum

if  $f'(c) = 0$  and  $f''(c) < 0$ ,  
 then  $c$  is a local maximum

Slant asymptotes are found by division

$x$ -intercepts  $(x, 0)$

$y$ -intercepts  $(0, y)$

DR  $M_2I_2$  ACIDS

Domain and Range

Maximums

Minimums

Intercepts

Inflection

Asymptotes

Concavity

Increasing

Decreasing

Symmetry

## Algebraic Relations

$$a^2 - b^2 = (a - b)(a + b)$$

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

sigma properties

$$\sum_{i=1}^n c = c + c + c + \dots + c = nc$$

$$\sum_{i=1}^n ct_i = c \sum_{i=1}^n t_i$$

$$\sum_{i=1}^n (t_i + s_i) = \sum_{i=1}^n t_i + \sum_{i=1}^n s_i$$

arithmetic series  $t_n = a + (n-1)d$

$$S_n = a + (a+d) + (a+2d) + \dots + [a + (n-1)d]$$

$$= \frac{n}{2}(2a + (n-1)d) = \frac{n(a + t_n)}{2}$$

geometric series  $t_n = ar^{n-1}$

$$S_n = a + ar + ar^2 + \dots + ar^{n-1}$$

$$= \frac{a(r^n - 1)}{r - 1} = \frac{rt_n - a}{r - 1}$$

$$S = \frac{a}{1-r}, \quad |r| < 1$$

natural numbers

$$\sum_{i=1}^n i = \frac{n(n+1)}{2}$$

natural number squares

$$\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$$

natural number cubes

$$\sum_{i=1}^n i^3 = \frac{n^2(n+1)^2}{4}$$

## Trigonometric Identities

### Reciprocal Identities

$$\csc x = \frac{1}{\sin x} \quad \sec x = \frac{1}{\cos x} \quad \cot x = \frac{1}{\tan x}$$

### Quotient Identities

$$\tan x = \frac{\sin x}{\cos x} \quad \cot x = \frac{\cos x}{\sin x}$$

### Pythagorean Identities

$$\sin^2 x + \cos^2 x = 1$$

$$\sec^2 x = 1 + \tan^2 x$$

$$\csc^2 x = 1 + \cot^2 x$$

### Sum and Difference Identities

$$\sin(x+y) = \sin x \cos y + \cos x \sin y$$

$$\sin(x-y) = \sin x \cos y - \cos x \sin y$$

$$\cos(x+y) = \cos x \cos y - \sin x \sin y$$

$$\cos(x-y) = \cos x \cos y + \sin x \sin y$$

$$\tan(x+y) = \frac{\tan x + \tan y}{1 - \tan x \tan y}$$

$$\tan(x-y) = \frac{\tan x - \tan y}{1 + \tan x \tan y}$$

### Double Angle Identities

$$\sin 2x = 2 \sin x \cos x$$

$$\cos 2x = \cos^2 x - \sin^2 x$$

$$= 2 \cos^2 x - 1$$

$$= 1 - 2 \sin^2 x$$

$$\tan 2x = \frac{2 \tan x}{1 - \tan^2 x}$$

### Half Angle Identities

$$\cos \frac{x}{2} = \pm \sqrt{\frac{1}{2} + \frac{\cos x}{2}}$$

$$\sin \frac{x}{2} = \pm \sqrt{\frac{1}{2} - \frac{\cos x}{2}}$$

### Related Angle Identities

$$\sin(\pi - x) = \sin x \quad \sin(2\pi - x) = -\sin x$$

$$\cos(\pi - x) = -\cos x \quad \cos(2\pi - x) = \cos x$$

$$\tan(\pi - x) = -\tan x \quad \tan(2\pi - x) = -\tan x$$

$$\sin(\pi + x) = -\sin x \quad \sin(-x) = -\sin x$$

$$\cos(\pi + x) = -\cos x \quad \cos(-x) = \cos x$$

$$\tan(\pi + x) = \tan x \quad \tan(-x) = -\tan x$$

### Correlated Angle Identities

$$\sin\left(\frac{\pi}{2} - x\right) = \cos x \quad \sin\left(\frac{3\pi}{2} - x\right) = -\cos x$$

$$\cos\left(\frac{\pi}{2} - x\right) = \sin x \quad \cos\left(\frac{3\pi}{2} - x\right) = -\sin x$$

$$\tan\left(\frac{\pi}{2} - x\right) = \cot x \quad \tan\left(\frac{3\pi}{2} - x\right) = \cot x$$

$$\sin\left(\frac{\pi}{2} + x\right) = \cos x \quad \sin\left(\frac{3\pi}{2} + x\right) = -\cos x$$

$$\cos\left(\frac{\pi}{2} + x\right) = -\sin x \quad \cos\left(\frac{3\pi}{2} + x\right) = \sin x$$

$$\tan\left(\frac{\pi}{2} + x\right) = -\cot x \quad \tan\left(\frac{3\pi}{2} + x\right) = -\cot x$$

### Limits of Trigonometric Functions

$$\lim_{\theta \rightarrow 0} \sin \theta = 0$$

$$\lim_{\theta \rightarrow 0} \cos \theta = 1$$

$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

$$\lim_{\theta \rightarrow 0} \frac{\cos \theta - 1}{\theta} = 0$$

$$\lim_{\theta \rightarrow 0} \frac{\theta}{\sin \theta} = 1$$

$$\lim_{\theta \rightarrow 0} \frac{1 - \cos \theta}{\theta} = 0$$

### Derivatives of Trigonometric Functions

$$\frac{d}{dx} \sin x = \cos x$$

$$\frac{d}{dx} \cos x = -\sin x$$

$$\frac{d}{dx} \tan x = \sec^2 x$$

$$\frac{d}{dx} \csc x = -\csc x \cot x$$

$$\frac{d}{dx} \sec x = \sec x \tan x$$

$$\frac{d}{dx} \cot x = -\csc^2 x$$

### Derivative Applications in Economics

$C(x)$  = Cost Function

$C'(x)$  = Marginal Cost Function

$p(x)$  = Price or Demand Function

$R(x) = xp(x)$  = Revenue Function

$R'(x)$  = Marginal Revenue Function

$P(x) = R(x) - C(x)$  = Profit Function

$C'(x) = R'(x)$  = Maximum Profit

$c(x) = \frac{C(x)}{x}$  = Ave Cost Function

$C'(x) = \frac{C(x)}{x}$  = Average Cost Min

### Limits/Derivatives of Exponential Functions

$$y = b^x$$

$$y' = \lim_{h \rightarrow 0} \frac{b^{x+h} - b^x}{h} = b^x \lim_{h \rightarrow 0} \frac{b^h - 1}{h}$$

$$\lim_{h \rightarrow 0} \frac{e^h - 1}{h} = 1$$

$$\lim_{x \rightarrow 0} (1+x)^{\frac{1}{x}} = e = \lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)^n$$

$$\frac{d}{dx} e^x = e^x$$

$$\frac{d}{dx} e^u = e^u \frac{du}{dx}$$

$$\frac{d}{dx} e^{g(x)} = e^{g(x)} g'(x)$$

$$\frac{d}{dx} b^x = b^x \ln b \quad \frac{d}{dx} b^u = b^u \ln b \frac{du}{dx}$$

Exponential Growth and Decay  
rate is proportional to amount

$$\frac{dy}{dt} = ky \text{ is solved } (k) \text{ with } y = y_0 e^{kt}$$

### Compound Interest

$$A = Pe^{rt}$$

$$A = P \left(1 + \frac{r}{n}\right)^{nt}$$

### Limits/Derivatives of Logarithmic Functions

$$y = \ln x$$

$$\frac{d}{dx} \ln x = \frac{1}{x}$$

$$\frac{d}{dx} \ln u = \frac{1}{u} \frac{du}{dx}$$

$$\frac{d}{dx} \log_b x = \frac{1}{x \ln b}$$

### Differential Equations

If  $y'' + ky = 0$ , then

$$y = A \cos(\sqrt{k}x) + B \sin(\sqrt{k}x)$$

Hooke's Law

$$s'' + \frac{k}{m}s = 0 \quad \frac{d^2s}{dt^2} + \frac{k}{m}s = 0 \quad F = ks$$

$$s = A \cos \sqrt{\frac{k}{m}} t + B \sin \sqrt{\frac{k}{m}} t$$

### Area

If  $y = f(x)$ , and  $f(x) > 0$ , then

$$A(b) = F(b) - F(a)$$

is the area under  $f(x)$  from  $a$  to  $b$

If  $y = \frac{1}{x}$ , and  $x > 1$ , then

$\ln x$  is the area under  $y$  from 1 to  $x$

If  $y = \frac{1}{x}$ , and  $0 < x < 1$ , then

$-\ln x$  is the area under  $y$  from  $x$  to 1

Trapezoid Rule

$$A = \frac{b-a}{2n} (f(a) + 2f(x_1) + \dots + 2f(x_{n-1}) + f(b))$$

### Integrals and Antiderivatives Definitions

Sum of Infinite Rectangles

$$\int_a^b f(x) dx = \lim_{\Delta x \rightarrow 0} \sum_{i=1}^b f(x_i) \Delta x$$

$$\text{where } \Delta x = \frac{b-a}{n} \text{ and } x_i = a + i \Delta x$$

Fundamental Theorem of Calculus

$$\int_a^b f(x) dx = F(b) - F(a)$$

### Integrals and Antiderivatives

General Rules

$$\int cf(x) dx = c \int f(x) dx$$

$$\int [f(x) + g(x)] dx = \int f(x) dx + \int g(x) dx$$

$$\int 0 dx = C$$

$$\int 1 dx = x + C \quad \int adx = ax + C$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C, \text{ when } n \neq -1$$

$$\int ax^n dx = \frac{ax^{n+1}}{n+1} + C, \text{ when } n \neq -1$$

$$\int \frac{1}{x} dx = \ln|x| + C \quad \int \frac{1}{x \ln b} dx = \log_b(|x|) + C$$

$$\int \sin x dx = -\cos x + C$$

$$\int \cos x dx = \sin x + C$$

$$\int \sec^2 x dx = \tan x + C$$

$$\int \csc^2 x dx = -\cot x + C$$

$$\int \sec x \tan x dx = \sec x + C$$

$$\int \csc x \cot x dx = -\csc x + C$$

$$\int e^x dx = e^x + C \quad \int b^x \ln b dx = b^x + C$$

$$\int a^x dx = \frac{a^x}{\ln a} + C, \text{ where } a \neq 1$$

$$\int \frac{1}{x^2 + 1} dx = \tan^{-1} x + C$$

$$\int \frac{1}{\sqrt{1-x^2}} dx = \sin^{-1} x + C$$

Substitution Rule

$$\int_a^b f(g(x))g'(x) dx = \int_{g(a)}^{g(b)} f(u) du, \text{ where } u = g(x)$$

### Integration Techniques

Fundamental Theorem of Calculus

$$\int_a^b f(x)dx = F(b) - F(a)$$

Substitution

$$\int_a^b f(g(x))g'(x)dx = \int_{g(a)}^{g(b)} f(u)du,$$

$$\text{where } u = g(x) \quad \text{and} \quad \frac{du}{dx} = g'(x)$$

or

$$\int F'(g(x))g'(x)dx = F(g(x)) + C$$

$$\text{where } \frac{d}{dx} F(g(x)) = F'(g(x))g'(x)$$

Partial Fractions

$$\int \frac{A(x)}{B(x)} dx = \int Q(x)dx + \int \frac{R(x)}{B(x)} dx$$

$$\int \frac{1}{\text{LIN}} dx, \text{ use normal methods}$$

$$\int \frac{A(x)}{B(x)} dx = \int \frac{A}{\text{LIN}} + \frac{B}{\text{LIN}} dx$$

$$\int \frac{A(x)}{(B(x))^n} dx = \int \frac{A}{B(x)} + \frac{B}{(B(x))^2} + \dots dx$$

$$\int \frac{A(x)}{B(x)} dx = \int \frac{Ax+B}{\text{QUAD}} + \frac{C}{\text{LIN}} dx$$

Integration by Parts

$$\int u dv = uv - \int v du$$

$$\int f(x)g'(x)dx$$

$$= f(x)g(x) - \int g(x)f'(x)dx$$

### Average Value of a Function

$$\text{Average Value} = \frac{\int_a^b f(x)dx}{(b-a)}$$

Volume of Rotation

$$V = \pi \int_a^b (f(x))^2 dx$$